

## Model Reduction of Dynamical Systems Exercise 1

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### Problem 1. *Image compression using SVD*

This is a programming exercise to understand the concept of singular value decomposition and how it can be used to compress an image. Download and save the script `computesvd.m` and the testimage `test.tif` from the course webpage [https://www.mpi-magdeburg.mpg.de/3668354/mor\\_ss19](https://www.mpi-magdeburg.mpg.de/3668354/mor_ss19).

- (a) Try different ranks for the low-rank representation and empirically determine the rank for which the compressed image resembles the original image. Obviously, there's no unique answer to this.
- (b) Check the compression in terms of memory, achieved by the SVD representation.

### Problem 2. *Laplace transform*

- (a) Find Laplace transform of the following functions:

(i)  $f(t) = 2t^2 - 3t + 5$ ,

(ii)  $f(t) = t^2 e^{-2t}$ ,

(iii)  $f(t) = \sin(2t) \cos(2t)$ ,

(iv)  $f(t) = \sin(2t) + e^{-3t} \cos(2t)$ .

- (b) Invert each of the following Laplace transforms:

(i)  $F(s) = \frac{4}{s^5}$ ,

(ii)  $F(s) = \frac{32}{s(s^2+16)}$ .

- (c) Using Laplace transform, solve the following ordinary differential equations:

(i)  $\ddot{x}(t) + x(t) = t$ ,  $x(0) = 0$ ,  $\dot{x}(0) = 2$ ,

(ii)  $\ddot{x}(t) + 2\dot{x}(t) + 5x(t) = 8e^{-3t}$ ,  $x(0) = \dot{x}(0) = 0$ .

**Extra:** Use the symbolic toolbox of MATLAB to determine Laplace transforms.